



Benha University
Benha Higher Institute of Technology
Department of Mechanical Eng.
Subject : Turbo machines Date: 8/1/2014
Model Answer of the Final Exam

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نموذج الإجابة المادة: اقتصاد هندسي م ٥٦١ الغرفة الخامسة
التاريخ الخميس ٨ يناير ٢٠١٥
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PROBLEM 1

After 2-years the future value of borrowed money will be $F = P(F/P, r, n) = P e^{rn} = 45000 \times 1.2712 = 57,206$

The continuous interest rate of one month = $e^{0.01} - 1 = 0.01005$
= $P (A/P, i, n) = P \{ [i(1+i)^n] / [(1+i)^n - 1] \}$ Capital Recovery A

A = $57,206 \times \{ [0.01005(1.01005)^{60}] / [(1.01005)^{60} - 1] \} = 57,206(0.01005 \times 1.8221 / 0.8221) = \1274.25

Problem 2

i) Total investment

$$P_A = \$650000 + 91,810 \times (P/A, 15, 5) = \$957,765.4$$

$$P_B = \$780000 + 53,569 \times (P/A, 15, 5) = \$959,574$$

$$P_C = \$600000 + 105000 \times (P/A, 15, 5) = \$951,981$$

$$P_D = \$720000 + 74000 \times (P/A, 15, 5) = \$968,062.8$$

Chose C as minimum cost.

ii) Use incremental analysis

Construct the table in ascending way

Without inflation

| | YEAR | C | A | D | B | A-C | D-C | B-C | |
|--------------|------|-----------|----------|----------|----------|----------|----------|------------|--|
| Initial Cost | 0 | \$600000 | \$650000 | \$720000 | \$780000 | -\$50000 | -\$12000 | -\$180,000 | |
| O&M | 1 | \$105,000 | \$91,810 | \$74,000 | \$53,569 | \$13,190 | \$31,000 | \$51,431 | |
| O&M | 2 | \$105,000 | \$91,810 | \$74,000 | \$53,569 | \$13,190 | \$31,000 | \$51,431 | |
| O&M | 3 | \$105,000 | \$91,810 | \$74,000 | \$53,569 | \$13,190 | \$31,000 | \$51,431 | |
| O&M | 4 | \$105,000 | \$91,810 | \$74,000 | \$53,569 | \$13,190 | \$31,000 | \$51,431 | |
| O&M | 5 | \$105,000 | \$91,810 | \$74,000 | \$53,569 | \$13,190 | \$31,000 | \$51,431 | |

$$NPW_{(A-C)} = \$ -50000 + \$13190 \times (P/A, 15\%, 5) = \$ -50000 + \$13190 \times 3.3522 = \$ -5784.482$$

Choose C

$$NPW_{(D-C)} = \$ -120,000 + \$31,000 \times 3.3522 = \$ -16081.8$$

Choose C

$$NPW_{B-C} = -\$180,000 + \$51,431 \times 3.3522 = -\$7593$$

Choose C

When Inflation is considered

$$\text{Real interest rate } i' = (i-f)/(1+f) = 5.5\%$$

Use the formula to find P/A

$$(P/A, 5.5, 5) = 4.2702844756191049757290192861196$$

ii) Total investment

$$P_A = \$650,000 + 91,810 \times (P/A, 5.5\%, 5) = \$1,042,045.8$$

$$P_B = \$780,000 + 53,569 \times (P/A, 5.5\%, 5) = \$1,087,045.8$$

$$P_C = \$600,000 + 105,000 \times (P/A, 5.5\%, 5) = \$1,083,799.8$$

$$P_D = \$720,000 + 74,000 \times (P/A, 5.5\%, 5) = \$1,036,000$$

Considering Inflation Choice B is the best.

3) The total Marginal cost

| Year | Market value | Loss in Market value | Foregone interest | Operating Cost, \$ | Maintenance Cost, \$ | Salvage Value, \$ | Total Recovery Cost |
|------|--------------|----------------------|-------------------|--------------------|----------------------|-------------------|---------------------|
| 0 | \$60000 | | | | | | |
| 1 | 35,000 | -\$25000 | -\$6000 | -15,000 | -3000 | 35,000 | -\$49000 |
| 2 | 30,000 | -\$5000 | -\$3500 | -17,000 | -3000 | 30,000 | -\$28500 |
| 3 | 25,000 | -\$5000 | -\$3000 | -19,000 | -3000 | 25,000 | -\$30000 |
| 4 | 20,000 | -\$5000 | -\$2500 | -21,000 | -3000 | 20,000 | -\$31500 |
| 5 | 15,000 | -\$5000 | -\$2000 | -23,000 | -3000 | 15,000 | -\$33000 |

The life cost of one year is 49000

$$\text{The EUAC for two years is } = (49000 + 28500 / (1+i)) \times (A/P, 10\%, 2) = (49000 + 28500 / (1+i)) \times 5762 = (49000 + 25909) \times 0.5762 = -\$43162.6$$

$$\text{The EUAC for three years is } = (49000 + 28500 / (1+i) + 30000 \times (1+i)^{-2}) \times (A/P, 10\%, 3) = (49000 + 25909 + 25993.2) \times 0.4021 = -\$40090.3$$

$$\text{The EUAC for four years is } = (49000 + 28500 / (1+i) + 30000 \times (1+i)^{-2} + 31500 \times (1+i)^{-3}) \times (A/P, 10\%, 4) = (49000 + 25909 + 25993.2 + 23666.3) \times 0.3155 = -\$38922$$

$$\text{The EUAC for five years is } = (49000 + 28500 / (1+i) + 30000 \times (1+i)^{-2} + 31500 \times (1+i)^{-3} + 33000 \times (1+i)^{-4}) \times (A/P, 10\%, 5) = (49000 + 25909 + 25993.2 + 23666.3 + 22539.4) \times 0.2638 = -\$38409$$

Economic life is 5 years

| Year | Market value | EUAC of Capital recovery | Foregone interest | Operating Cost, \$ | Maintenance Cost, \$ | Salvage Value, \$ | Total Recovery Cost |
|------|--------------|--------------------------|-------------------|--------------------|----------------------|-------------------|---------------------|
| 0 | \$60000 | | | | | | |
| 1 | 35,000 | -\$25000 | -\$6000 | -15,000 | -3000 | 35,000 | -\$49000 |
| 2 | 30,000 | -\$5000 | -\$3500 | -17,000 | -3000 | 30,000 | -\$28500 |
| 3 | 25,000 | -\$5000 | -\$3000 | -19,000 | -3000 | 25,000 | -\$30000 |
| 4 | 20,000 | -\$5000 | -\$2500 | -21,000 | -3000 | 20,000 | -\$31500 |
| 5 | 15,000 | -\$5000 | -\$2000 | -23,000 | -3000 | 15,000 | -\$33000 |

For one year

$$\text{EUAC of Capital recovery for one year } = -\$60000 \times (A/P, 10\%, 1) + \$35000 \times (A/F, 10\%, 1) = -\$66000 + \$35000 = -\$31000$$

$$\text{EUAC of Capital recovery for two years } = -\$60000 \times (A/P, 10\%, 2) + \$30000 \times (A/F, 10\%, 2)$$

$$= -\$60000 \times 0.5762 + \$30000 \times 0.476 = -\$20292$$

$$\text{EUAC of Capital recovery for three years } = -\$60000 \times (A/P, 10\%, 3) + \$25000 \times (A/F, 10\%, 3)$$

$$= -\$60000 \times 0.4021 + \$25000 \times 0.3021 = -\$16573.5$$

$$\text{EUAC of Capital recovery for four years } = -\$60000 \times (A/P, 10\%, 4) + \$20000 \times (A/F, 10\%, 4)$$

$$= -\$60000 \times 0.3155 + \$20000 \times 0.2155 = -\$14620$$

$$\text{EUAC of Capital recovery for five years } = -\$60000 \times (A/P, 10\%, 5) + \$15000 \times (A/F, 10\%, 5)$$

$$= -\$60000 * 0.2638 + \$15000 * 0.1638 = -\$13371$$

| Year | Market value | EUAC of Capital recovery | Operating Cost,\$ | Maintenance Cost,\$ | Total EUAC |
|------|--------------|--------------------------|-------------------|---------------------|------------|
| 0 | \$60000 | | | | |
| 1 | 35,000 | -\$31000 | --15,000 | -3000 | -\$49000 |
| 2 | 30,000 | -\$20292 | -17,000 | -3000 | -\$40292 |
| 3 | 25,000 | -\$16573.5 | -19,000 | -3000 | --\$38573 |
| 4 | 20,000 | -\$14620 | -21,000 | -3000 | -\$38620 |
| 5 | 15,000 | -\$13371 | -23,000 | -3000 | --\$39391 |

| Year | Market value | EUAC of Capital recovery | EUAC OP cost,\$ | Maintenance Cost,\$ | Total EUAC |
|------|--------------|--------------------------|-----------------|---------------------|-------------|
| 0 | \$60000 | | | | |
| 1 | 35,000 | -\$31000 | --15,000 | -3000 | -\$49000 |
| 2 | 30,000 | -\$20292 | -15,932.4 | -3000 | -\$39224.4 |
| 3 | 25,000 | -\$16573.5 | -16873.2 | -3000 | --\$36446.7 |
| 4 | 20,000 | -\$14620 | -17636 | -3000 | -\$35256 |
| 5 | 15,000 | -\$13371 | -18620 | -3000 | --\$34991 |

Economic life is 5 years

4)

Estimated salvage value = \$750. Giuliano's is in the 34% tax bracket.

SL depreciation = $(3000 - 750) / 5 = \$450$ per year.

| Year | CF before taxes | SL Depr. | Taxable Inc. | Tax (34%) | CF after taxes |
|------|-----------------|----------|-----------------|---------------|----------------|
| | (a) | (b) | (c) = (a) - (b) | (d) = -34%(c) | (a) + (d) |
| 0 | -\$3,000 | | | | -\$3,000 |
| 1 | 800 | 450 | 350 | -119 | 681 |
| 2 | 800 | 450 | 350 | -119 | 681 |
| 3 | 800 | 450 | 350 | -119 | 681 |
| 4 | 800 | 450 | 350 | -119 | 681 |
| 5 | 800 + 750 | 450 | 350 | -119 | 681 + 750 |

Before Taxes: CFS (a) has IRR = 15.69%

After Taxes: CFS (e) has IRR = 10.55%

After-tax analysis is what is most important.

Income taxes are a major disbursement that cannot be ignored.

Only the after-tax ROR is a meaningful value.

5)

Using the geometric gradient with real factor = $(1+i)/(1+f)$

$$= A (P/A, g, i, n) = A \{ [1 - (1+g)^n (1+i)^{-n}] / (i-g) \} \quad P \quad \text{If } i \neq g,$$

$$P = 1800 * 1.12^{-5} = -17843.8 = 1800 * 1.12 = \$19450$$

iii) Constant dollar

$$i' = (i-f)/(1+f) = 2.70229\%$$

$$= A (P/A, i, n) = A \{ [(1+i)^n - 1] / [i(1+i)^n] \} \quad \text{Present Worth: } P$$

$$P = 1800 * (1.12^{-5}) / (0.0275229 * 1.42327) = 1800 * 1.12^{-5} = 19450$$