



Answer the following questions:

Q1: Complete the following sentences:

- i. The family of FET transistors may be divided into: and
- ii. The MOSFET has a physical channel between the drain and source.
- iii. The high input resistance of a JFET is due to
- iv. The non-inverting configuration has a gain greater than or equal to
- v. The..... detectors can be used to produce a square wave from a sine wave.
- vi. The feedback element in an integrator is
- vii. The bandwidth of the ideal op amp is approximately equal to
- viii. The input stage of every op amp isamplifier.
- ix. When same signals are applied to the inputs of a differential amplifier it known as.....
- x. The input differential resistance of BJT differential amplifier is equal to
- xi. is a measure of a differential amplifier's ability to reject common mode signal.

Q2: (a) the NMOS transistors in the circuit of Fig. (1) have $V_t = 1V$, $\mu_n C_{ox} = 120 \mu A/V^2$, $\lambda = 0$, and $L_1=L_2= L_3 = 1\mu m$. Find the required values of gate width for each of Q_1 , Q_2 , and Q_3 to obtain the voltages and current values indicated.

(b) Find the input resistance of the circuit shown in Fig.(2). Assuming ideal op amp, $R_1 = 10 k\Omega$, $R_2 = 100 k\Omega$, and $R_3 = 5 k\Omega$.

Q3: A common gate amplifier using an n-channel E-MOS transistor for which $g_m=5mA/V$, shown in Fig.(3), has $R_D=5K\Omega$, and $R_L=2 K\Omega$. The amplifier is driven by voltage source having a 200Ω resistance. What are the input resistance and the overall voltage gain of the amplifier? If the circuits allow a bias current increase by a factor of 4 while maintaining linear operation, what do the input resistance and voltage gain become?

Q4: The two op amps in the circuit shown in fig.(4) are ideal. Find v_o , i_x and i_o .

Q5: Find the overall voltage gain v_o/v_s and the differential input resistance of the amplifier shown in fig. (5). Assuming $\beta = 100$.

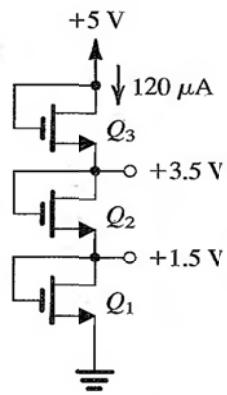


Fig.(1)

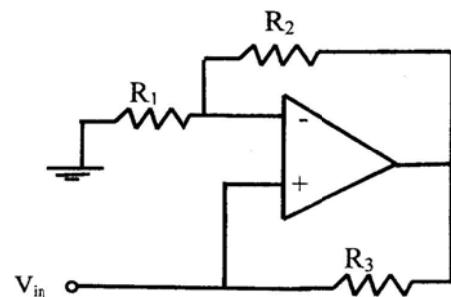


Fig.(2)

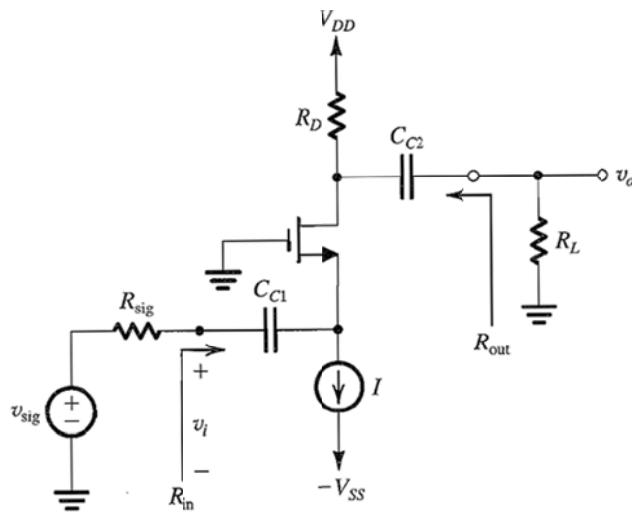


Fig.(3)

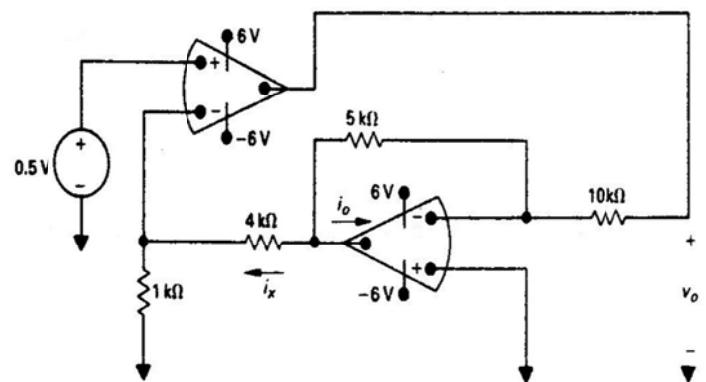


Fig.(4)

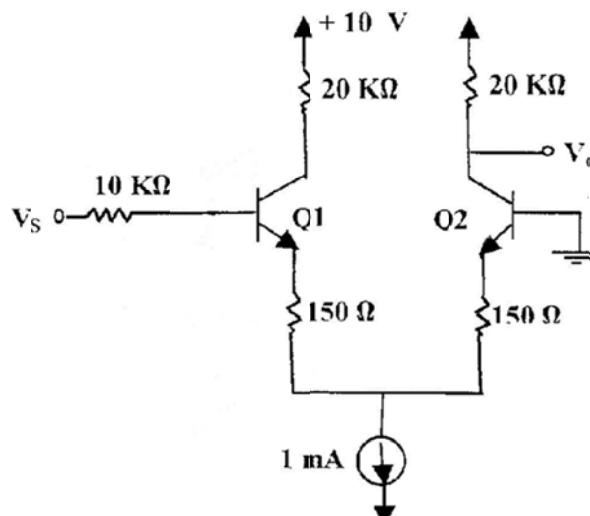


Fig.(5)

BEST WISHES

Hossam Labib



Model Answer

Q1: Complete the following sentences:

- i. The family of FET transistors may be divided into: Junction FET (JFET) and Metal-Oxide-Semiconductor FET (MOSFET)
- ii. The depletion MOSFET has a physical channel between the drain and source.
- iii. The high input resistance of a JFET is due to the reverse-biased gate source junction.
- iv. The non-inverting configuration has a gain greater than or equally one.
- v. The zero crossing detectors can be used to produce a square wave from a sine wave.
- vi. The feedback element in an integrator is a capacitor.
- vii. The bandwidth of the ideal op amp is approximately equal to ∞ .
- viii. The input stage of every op amp is a differential amplifier.
- ix. When same signals are applied to the inputs of a differential amplifier it known as common mode signal.
- x. The input differential resistance of BJT differential amplifier is equal to $(1+\beta)2r_e$
- xi. CMRR is a measure of a differential amplifier's ability to reject common mode signal.

Q2: (a) the NMOS transistors in the circuit of Fig. (1) have $V_t = 1V$, $\mu_n C_{ox} = 120 \mu A/V^2$, $\lambda = 0$, and $L_1 = L_2 = L_3 = 1\mu m$. Find the required values of gate width for each of Q_1, Q_2 , and Q_3 to obtain the voltages and current values indicated.

Solution

$$I_{D1} = I_{D2} = I_{D3} = 120 \text{ mA}$$

For Q_1

$$V_{S1} = 0 \quad \& \quad V_{G1} = V_{D1} = 1.5 \text{ V}$$

$$V_{GS1} = V_{G1} - V_{S1} = 1.5 \text{ V}$$

$$V_{DS1} = V_{D1} - V_{S1} = 1.5 \text{ V}$$

$$V_{DS1|_{sat}} = V_{GS1} - V_t = 1.5 - 1 = 0.5 \text{ V}$$

$\therefore V_{DS1} > V_{DS1|_{sat}}$ $\therefore Q_1$ in Saturation Region

$$I_{D1} = K_1 (V_{GS1} - V_t)^2$$

$$K_1 = \frac{I_{D1}}{(V_{GS1} - V_t)^2} = \frac{120 \text{ mA}}{(0.5)^2} = 480 \text{ mA/V}^2$$

$$\therefore K_1 = \frac{1}{2} \mu n C_{ox} \times \frac{W_1}{L_1} \Rightarrow W_1 = \frac{2 K_1 L_1}{\mu n C_{ox}}$$

$$W_1 = \frac{2 * 480 * 10^{-6} * 1 * 10^{-6}}{120 * 10^{-6}} = 8 \mu \text{m}$$

For Q_2

$$V_{S2} = 1.5 \text{ V} ; V_{G2} = V_{D2} = 3.5 \text{ V}$$

$$V_{GS2} = V_{G2} - V_{S2} = 3.5 - 1.5 = 2 \text{ V}$$

$$V_{DS2} = V_{D2} - V_{S2} = 3.5 - 1.5 = 2 \text{ V}$$

$$V_{DS2|_{sat}} = V_{GS2} - V_t = 2 - 1 = 1 \text{ V}$$

$V_{DS2} > V_{DS2|_{sat}}$ $\Rightarrow Q_2$ in Saturation Region

$$K_2 = \frac{I_{D2}}{(V_{GS2} - V_t)^2} = \frac{120 \text{ mA}}{(1)^2} = 120 \text{ mA/V}^2$$

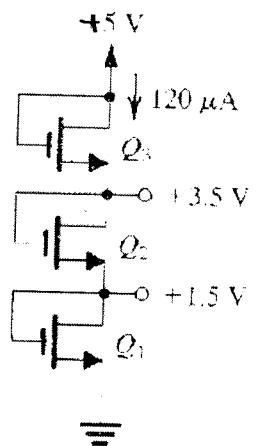
$$W_2 = \frac{2 K_2 L_2}{\mu n C_{ox}} = \frac{2 * 120 * 10^{-6} * 10^{-6}}{120 * 10^{-6}} = 2 \mu \text{m}$$

For Q_3 $V_{S3} = 3.5 \text{ V} ; V_{G3} = V_{D3} = 5 \text{ V}$

$$V_{GS3} = V_{G3} - V_{S3} = 5 - 3.5 = 1.5 \text{ V} = V_{DS3} \Rightarrow Q_3$$
 in Saturation

$$K_3 = \frac{I_{D3}}{(V_{GS3} - V_t)^2} = \frac{120 \text{ mA}}{(0.5)^2} = 480 \text{ mA/V}^2$$

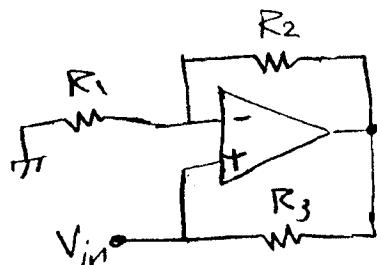
$$\Rightarrow W_3 = W_1 = 8 \mu \text{m}$$



(2)

Q2:(b) (6 Points)

Find The input resistance R_{in} of the circuit shown. Assume ideal op Amp. and $R_1 = 10\text{ k}\Omega$, $R_2 = 100\text{ k}\Omega \rightarrow R_3 = 5\text{ k}\Omega$.



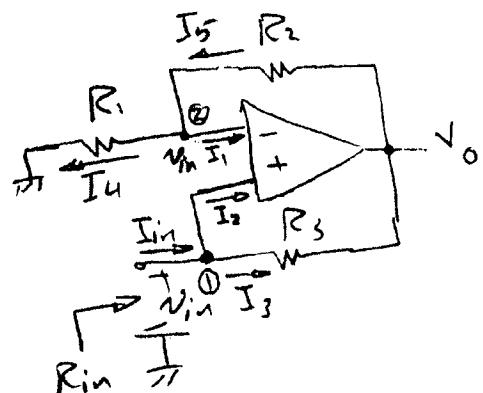
Solution

Apply ΔILP voltage and evaluate the ΔILP current I_{in} thus

$$R_{in} = \frac{V_{in}}{I_{in}}$$

at node (1)

$$I_{in} = I_2 + I_3 \quad ; \quad I_1 = I_2 = 0$$



$$I_{in} = I_3 = \frac{V_{in} - V_0}{R_3} \rightarrow (1) ; \quad V^+ = V^- = V_{in}$$

at node (2)

$$I_5 = I_4 + I_1 \quad ; \quad I_1 = 0$$

$$I_5 = I_4 \Rightarrow \frac{V_1 - 0}{R_1} = \frac{V_0 - V}{R_2}$$

$$\frac{V_{in}}{R_1} = \frac{V_0 - V_{in}}{R_2} \Rightarrow V_{in} \left(\frac{1}{R_1} + \frac{1}{R_2} \right) = \frac{V_0}{R_2}$$

$$V_0 = V_{in} \left(1 + \frac{R_2}{R_1} \right) \rightarrow (2)$$

$$\text{From (1)} \Rightarrow I_{in} = \frac{V_{in}}{R_3} - \frac{V_0}{R_3} = \frac{V_{in}}{R_3} - \frac{V_{in}}{R_3} \left(1 + \frac{R_2}{R_1} \right)$$

$$I_{in} = \frac{V_{in}}{R_3} \left(1 - 1 - \frac{R_2}{R_1} \right) = \frac{V_{in}}{R_3} \left(-\frac{R_2}{R_1} \right)$$

$$\therefore R_{in} = \frac{V_{in}}{I_{in}} = -R_3 \left(\frac{R_1}{R_2} \right) \quad [\text{this circuit is called negative Impedance converter (NIC)}]$$

$$R_{in} = - \left(\frac{5\text{ k} \times 10\text{k}}{100\text{k}} \right) = -0.5\text{ k}\Omega$$

(3)

Q3: A common gate amplifier using an n-channel E-MOS transistor for which $g_m = 5 \text{ mA/V}$, shown in Fig., has $R_D = 5 \text{ k}\Omega$, and $R_L = 2 \text{ k}\Omega$. The amplifier is driven by voltage source having a 200Ω resistance. What are the input resistance and the overall voltage gain of the amplifier? If the circuits allow a bias current increase by a factor of 4 while maintaining linear operation, what do the input resistance and voltage gain become?

Solution:

$$g_m = 5 \text{ mA/V}$$

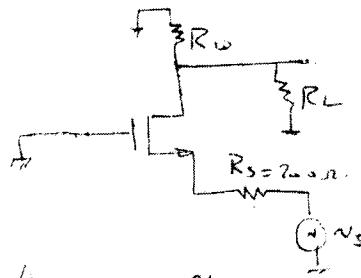
$$R_L = 2 \text{ k}\Omega \quad R_D = 5 \text{ k}\Omega$$

$$R_S = 200\Omega$$

AC analysis

All capacitors S.C.

reduce dc sources i.e. $v_s = \text{S.C.} + \text{C.S.} = 0$



$$\text{To find } A_v = \frac{v_o}{v_s}$$

$$v_o = -g_m v_{gs} (R_D \parallel R_L)$$

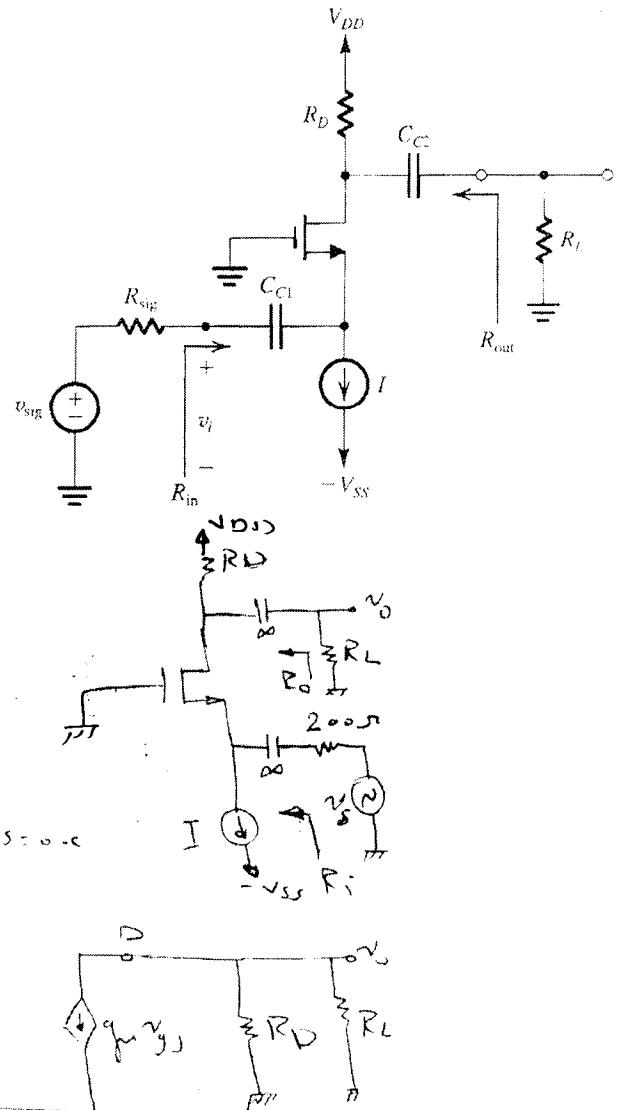
$$-v_{gs} = g_m v_{gs} R_s + v_s$$

$$v_{gs}(1 + g_m R_s) = -v_s$$

$$v_{gs} = \frac{-v_s}{1 + g_m R_s}$$

$$v_o = +g_m \frac{v_s}{1 + g_m R_s} (R_D \parallel R_L)$$

$$\frac{v_o}{v_s} = +\frac{g_m}{1 + g_m R_s} (R_D \parallel R_L) = \frac{5 \times 10^{-3}}{1 + 200 \times 5 \times 10^{-3}} (2 \text{ k}\Omega \parallel 5 \text{ k}\Omega) = 3.57$$



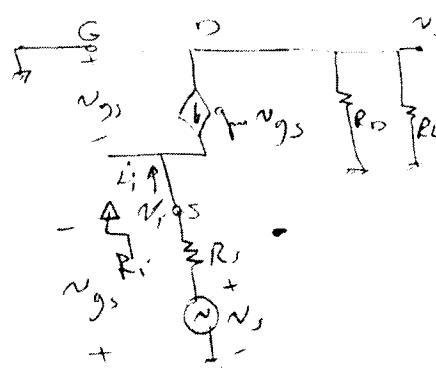
$$R_i = \frac{v_i}{i_i}$$

$$L_i = -\alpha_{gss} v_{gs}$$

$$v_i = -v_{gs}$$

$$\therefore R_i = \frac{-v_{gs}}{-\alpha_{gss} v_{gs}} = \frac{1}{\alpha_{gss}}$$

$$= \frac{1}{5 \times 10^{-3}} = 200 \Omega$$



(b)

$$\therefore \alpha_m = 2\sqrt{K I_{D_s}}$$

$$\alpha_{m_1} = 2\sqrt{K S_{D_1}}, \quad ; \quad \alpha_{m_2} = 5 \text{ mA/V}$$

If I_D increase by factor 4 $\Rightarrow I_{D_2} = 4 I_{D_1}$

$$\therefore \alpha_{m_2} = 2\sqrt{K I_{D_2}} = 2\sqrt{K \times 4 I_{D_1}} = 2(2\sqrt{K S_{D_1}})$$

$$\alpha_{m_2} = 2 \alpha_{m_1} = 2 \times 5 = 10 \text{ mA/V}$$

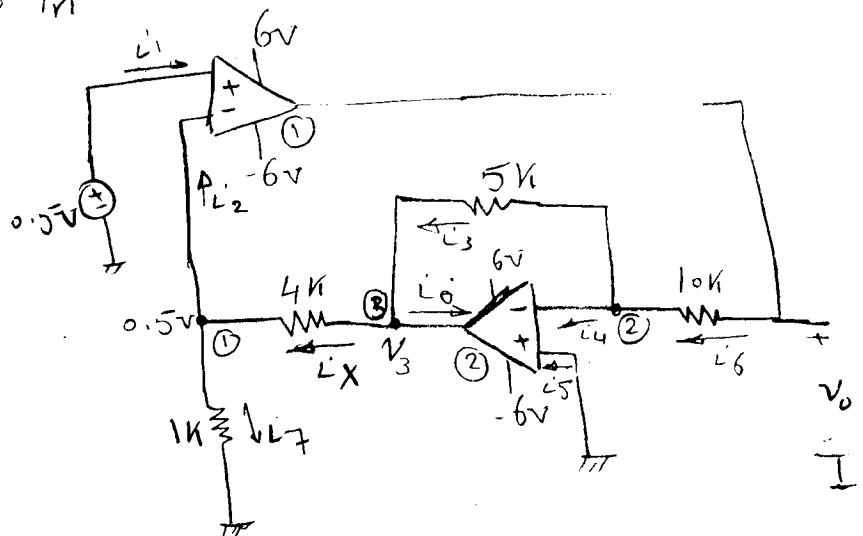
$$\therefore R_i = \frac{1}{\alpha_{m_2}} = \frac{1}{10 \text{ mA}} = 100 \Omega$$

$$\frac{v_o}{v_s} = \frac{\alpha_{m_2}}{1 + \alpha_{m_2} R_S} (R_D || R_L)$$

$$= \frac{10 \times 10^{-3}}{1 + 10 \times 10^{-3} \times 2} \cdot (2 \text{ nA} / 5 \text{ K}) = 4.76 \text{ V/V}$$

⑤

Q4: The two opamps in the circuit shown are ideal. Find V_o , i_x and i_o



Solution

$$\text{For opamp } 1 \Rightarrow V_1^+ = V_1^- = 0.5V$$

$$i_1 = i_2 = 0$$

at node 1

$$i_2 + i_7 = i_x \quad ; \quad i_2 = 0$$

$$i_x = i_7 \Rightarrow i_x = \frac{0.5}{1K} = 0.5 \text{ mA}$$

$$\text{For opamp } 2 \Rightarrow V_2^+ = V_2^- = 0 \quad ; \quad i_4 = i_5 = 0$$

at node 2

$$i_6 = i_3 + i_4 \quad ; \quad i_4 = 0$$

$$i_6 = i_3 \Rightarrow \frac{V_o - V_2^-}{10K} = \frac{V_2^- - V_3}{5K} \Rightarrow \frac{V_o}{10K} = -\frac{V_3}{5K} \quad *5K$$

$$0.5V_o = -V_3 \Rightarrow V_o = -2V_3 \rightarrow \boxed{\text{D}}$$

$$\therefore V_3 = i_x \times 4K + 0.5V = 0.5mA \times 4K + 0.5 = 2.5V$$

$$V_o = -2 \times 2.5 = -5V \quad \Rightarrow \boxed{V_o = -5V}$$

at node 3

$$i_3 = i_0 + i_x \Rightarrow i_0 = i_3 - i_x$$

$$i_0 = \frac{-V_3}{5K} - 0.5mA = \frac{-2.5}{5K} - 0.5mA = -0.5mA - 0.5mA$$

$$i_0 = -1mA$$

Q5:-

Find the overall voltage gain V_o/V_s and the differential input resistance of the amplifier shown. Assuming $\beta = 100$

Solution

DC Analysis

$$I_{E_1} = I_{E_2} = I_E = \frac{I}{2}$$

$$I_E = \frac{1 \text{ mA}}{2} = 0.5 \text{ mA} \rightarrow 2$$

$$I_C = \alpha I_E = 0.99 I_E$$

$$= 0.99 \times 0.5 \text{ mA} = 0.495 \text{ mA} \approx 0.5 \text{ mA}$$

$$V_T = \frac{V_T}{I_E} = \frac{25 \text{ mV}}{0.5 \text{ mA}} = 50 \Omega \rightarrow 1$$

$$g_m = \frac{I_C}{V_T} = \frac{0.5 \text{ mA}}{25 \text{ mV}} = 20 \text{ mA/V}$$

$$r_{\pi} = \frac{B}{g_m} = \frac{100}{20 \text{ mA}} = 500 \text{ ohm} = 5 \text{ k}\Omega.$$

$$R_{id} = (1 + B) (2R_E + 2r_e) = (1 + 100) (2 \times 150 + 2 \times 50) = 40.4 \text{ k}\Omega \rightarrow 3$$

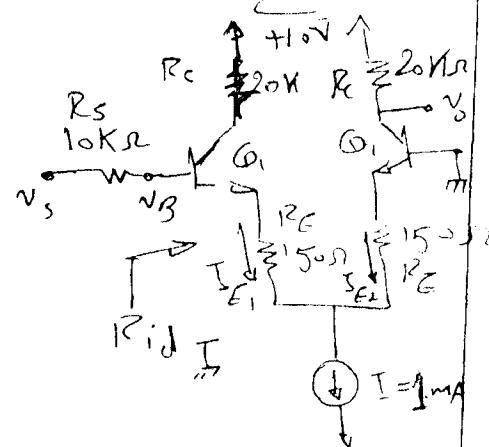
$$\frac{V_o}{V_s} = \frac{V_o}{V_B} \times \frac{V_B}{V_s} \rightarrow 1$$

$$\frac{V_o}{V_B} = \frac{R_C}{2R_E + 2r_e} = \frac{20 \text{ k}\Omega}{2 \times 150 + 2 \times 50} = 50 \rightarrow 2$$

$$N_D = \frac{R_{id}}{R_{id} + R_s}$$

$$\frac{V_B}{V_s} = \frac{R_{id}}{R_{id} + R_s} = \frac{40.4 \text{ k}\Omega}{(40.4 \text{ k}\Omega + 10) \text{ k}\Omega} = 0.802 \rightarrow 1$$

$$\frac{V_o}{V_s} = 0.802 \times 50 = 40.1 \rightarrow 2$$



(7)