



Time: Three Hours (attempt all questions) (assume any missing data)

Q1 (20 points)

1- 1) Explain the pump cavitation, what are the signs of pump Cavitations and discuss its influence upon runner-dynamic machines?

Solution

Pump cavitation is the formation and subsequent collapse or implosion of vapor bubbles in a pump. It occurs when gas bubbles are formed in the pump due to drop in absolute pressure of the liquid below vapor pressure.

- | | | |
|----------|--------------|-----------------------|
| 1. Noise | 2. Vibration | 3. Fluctuating gauges |
|----------|--------------|-----------------------|
1. Pitting damage to the impeller
 2. Sharp drop in pump head and disharg
 3. Sudden drop for the efficiency

1- 2) The characteristics of a single stage single suction centrifugal pump running at a speed of 950 rpm are as follows:

Q (lit/sec)	0	50	100	150	200	250	300
H (m of water)	33.5	35	36	35.5	34	29.5	21
BP (kW)	20.6	36.8	53	67	82.5	95.5	100

On a certain occasion the pump is required to deliver 130 lit/sec against a total head of the pump of 30 m.

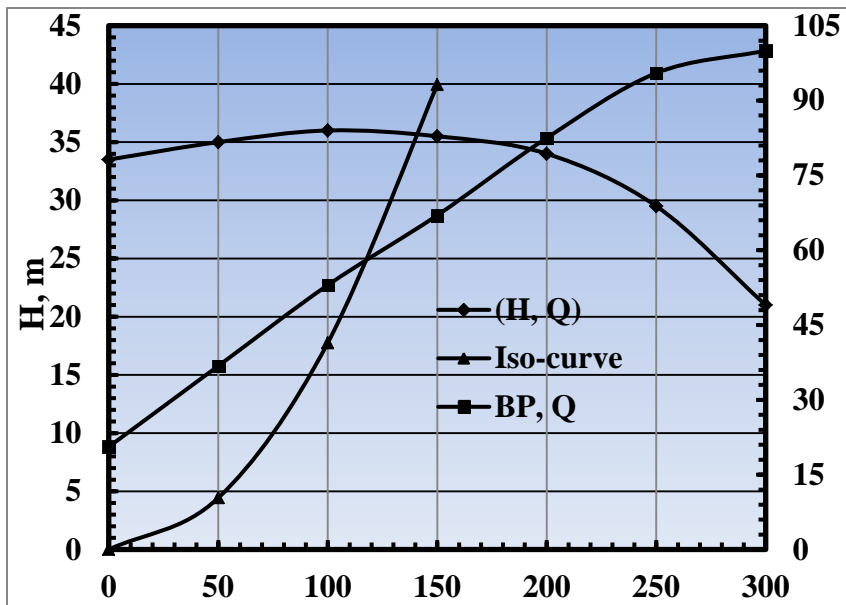
Determine:

- The new speed of the pump.
- The corresponding power input.
- The specific speed of this pump.
- Calculate the head coefficient C_H , discharge coefficient C_Q , power coefficient C_p if the pump diameters 30cm.

Solution

- By Iso-efficiency curve

$$H \propto Q^2, \quad \therefore H = kQ^2, \quad k = \frac{H}{Q^2} = \frac{30}{130^2} = 0.001775 \frac{m \cdot s^2}{lit^2}$$



From iso-curve and H - Q curve.

$Q_{p1} = 140 \text{ L/s}$	$H_{p1} = 36 \text{ m}$	$BP_1 = 68 \text{ kW}$	$N_{p1} = 950 \text{ rpm}$
$Q_{p2} = 130 \text{ L/s}$	$H_{p2} = 30 \text{ m}$	$BP_2 = ?? \text{ kW}$	$N_{p1} = ?? \text{ rpm}$

$$C_{Q1} = C_{Q2}$$

$$\frac{Q_{p1}}{N_{p1} * D_{p1}^3} = \frac{Q_{p2}}{N_{p2} * D_{p2}^3} \quad \therefore \frac{Q_{p1}}{N_{p1}} = \frac{Q_{p2}}{N_{p2}}$$

$$N_{p2} = \frac{Q_{p2}}{Q_{p1}} * N_{p1} = \frac{130}{140} * 950 = 882 \text{ rpm}$$

$$C_{p1} = C_{p2}$$

$$\frac{BP_{p1}}{N_{p1}^3 * \rho * D_{p1}^5} = \frac{BP_{p2}}{N_{p2}^3 * \rho * D_{p2}^5} \quad \therefore \frac{BP_{p1}}{N_{p1}^3} = \frac{BP_{p2}}{N_{p2}^3}$$

$$BP_{p2} = \frac{BP_{p1}}{N_{p1}^3} * N_{p2}^3 = \left(\frac{N_{p2}}{N_{p1}}\right)^3 * BP_{p1} = \left(\frac{882}{950}\right)^3 * 68 = 54.4 \text{ kW}$$

$$N_s = \frac{N \sqrt{Q}}{(H)^{3/4}} = \frac{882 \sqrt{0.13}}{(30)^{3/4}} = 24.8$$

$$C_{Q1} = \frac{Q_{p1}}{N_{p1} * D_{p1}^3} = \frac{0.14}{\left(\frac{950}{60}\right) * (0.3)^3} = 0.327$$

$$C_{H1} = \frac{gH_{p1}}{N_{p1}^2 * D_{p1}^2} = \frac{9.81 * 36}{\left(\frac{950}{60}\right)^2 * (0.3)^2} = 15.65$$

$$C_{p1} = \frac{BP_{p1}}{N_{p1}^3 * \rho * D_{p1}^5} = \frac{68 * 1000}{1000 * \left(\frac{950}{60}\right)^3 * (0.3)^5} = 0.62$$

Q2 (20 points)

2-1) Explain with sketch different types of compressors?

Solution

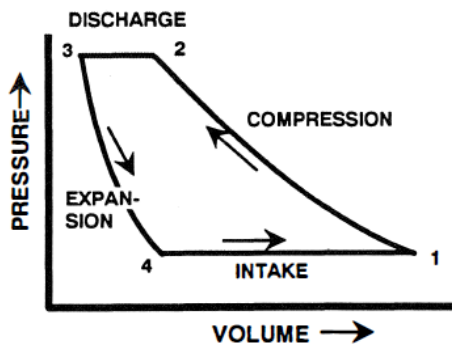
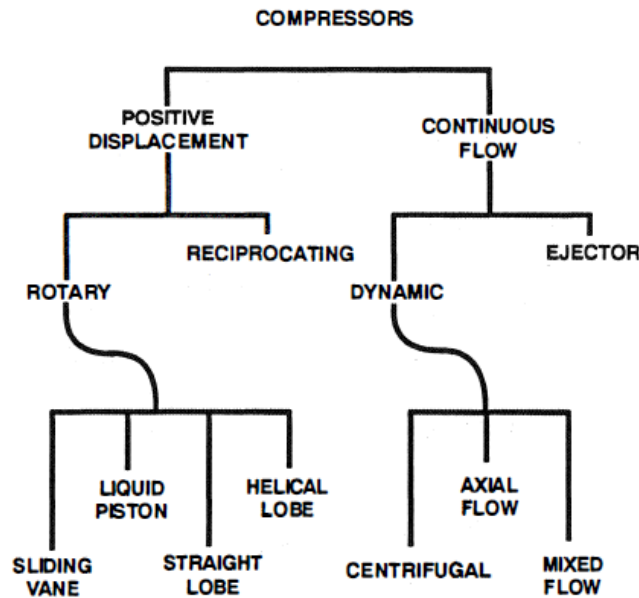


Figure 2. Reciprocating Compressors.

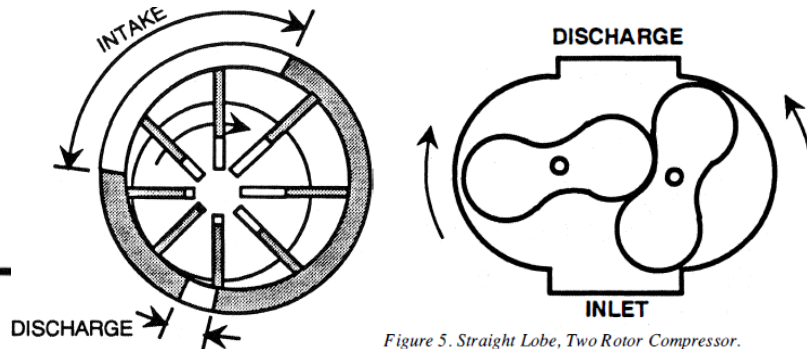


Figure 5. Straight Lobe, Two Rotor Compressor.

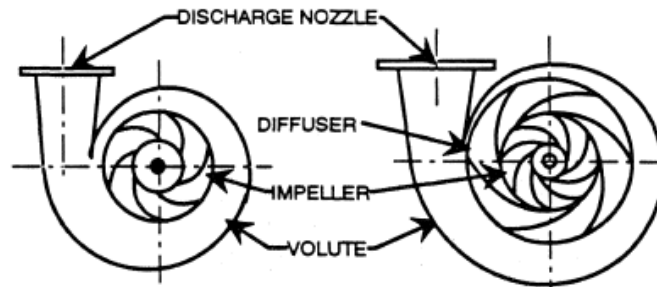


Figure 7. Centrifugal Compressors.

2-2) The velocity of steam at inlet to a simple impulse turbine is 1000 m/s, and the nozzle angle is 20° . The blade speed is 400 m/s and the blades are symmetrical. **Determine** the blade angles if the steam is to enter the blades without shock. If the friction effects on the blade are negligible, calculate:

- i) Input power and the diagram power for a mass flow of 0.75 kg/s.
- ii) The axial thrust and the diagram efficiency.
- iii) Speed ratio and the speed of rotation if the mean diameter of the wheel is 500 mm.
- iv) The output power at maximum diagram efficiency and the maximum diagram efficiency if the absolute velocity remains constant.

Solution

- ✓ For symmetrical blades then $\beta_i = \beta_e$
- ✓ For friction effects on the blade are negligible then $C_{ri} = C_{re}$

i) Applying the cosine rule to triangle OAB

$$C_{ri}^2 = C_{ai}^2 + C_b^2 - 2 C_{ai} C_b \cos \alpha_i$$

$$C_{ri}^2 = 1000^2 + 400^2 - (2 * 1000 * 400 * \cos 20)$$

$$C_{ri}^2 = 40.8 * 10^4$$

$C_{ri} = 639 \text{ m/s} = C_{re}$

and by using sine rule in OAB

$$\frac{C_{ai}}{\sin OAB} = \frac{C_{ri}}{\sin \alpha_i}$$

Also $\sin OAB = \sin (180 - \beta_i) = \sin \beta_i$

$$\therefore \frac{C_{ai}}{\sin \beta_i} = \frac{C_{ri}}{\sin \alpha_i}$$

$$\therefore \sin \beta_i = \left(\frac{C_{ai}}{C_{ri}} \right) \sin \alpha_i = \frac{1000 * \sin 20}{639} = 0.535$$

$\beta_i = 32.3 = \beta_e$

$AD = C_{ri} \cos \beta_i = 639 \cos 32.3 = 540 \text{ m/s}$

$AE = C_{re} \cos \beta_e = 639 \cos 32.3 = 540 \text{ m/s}$

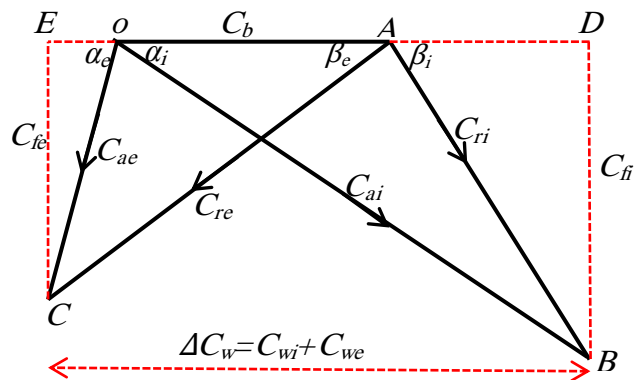
$\Delta C_w = 540 + 540 = 1080 \text{ m/s}$

$Input Power = \dot{m} \frac{C_{ai}^2}{2} = 0.75 * \frac{1000^2}{2} = 375 \text{ kw}$

$diagram Power = \dot{m} C_b \Delta C_w = 0.75 * 400 * 1080 = 324 \text{ kw}$

$diagram Efficiency = \frac{diagram Power}{Input Power} = \frac{324}{375} = 86.4\%$

$C_{fi} = C_{ri} \sin \beta_i = 639 \sin 32.3 = 341.4 \text{ m/s}$



$$C_{fe} = C_{re} \sin \beta_e = 639 \sin 32.3 = 341.4 \text{ m/s}$$

$$\Delta C_f = C_{fi} - C_{fe} = 0$$

Axial thrust = 0

$$\text{Speed ratio} = C_b / C_{ai} = 400/1000 = 0.4$$

$$C_b = (\pi DN/60)$$

$$\text{speed of rotation} = N = 60 \cdot 400 / (\pi \cdot 0.5) = 15278.8 \text{ rpm}$$

max.

$$\begin{aligned} \text{max. diagram Power} &= \dot{m} \left(\frac{\cos \alpha_i}{2} \right) C_{ai} \Delta C_w = 0.75 \cdot \frac{0.9}{2} \cdot 1080 \cdot 1000 \\ &= 380 \text{ kw} \end{aligned}$$

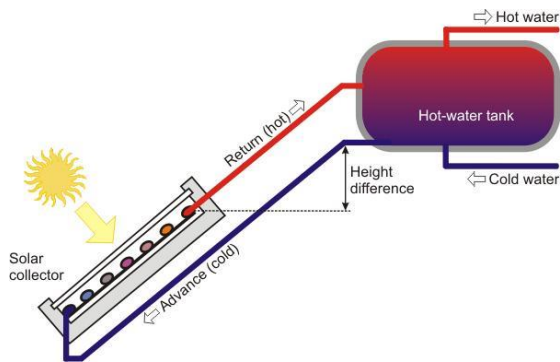
$$\text{max. diagram effici.} = \cos \alpha_i = \cos 20 = 94\%$$

Q3 (20 points)

3-1) Explain briefly with the aid of sketch the different types of solar water collectors?

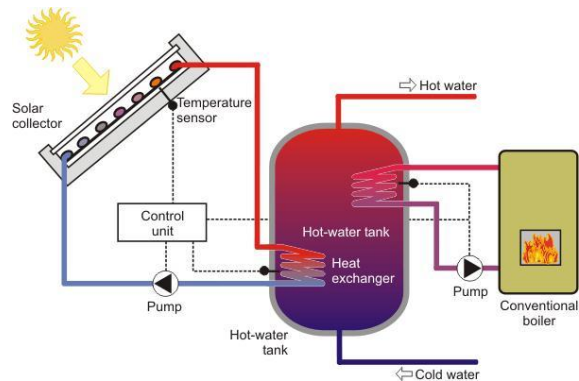
Solution

Thermosyphon systems



The principle of the thermosyphon system is that cold water has a higher specific density than warm water, and so being heavier will sink down.

Forced-circulation systems



In contrast to thermosyphon systems, an electrical pump can be used to move water through the solar cycle of a system by forced circulation. Collector and storage tank can then be installed independently, and no height difference between tank and collector is necessary.

3-2) A 2-shell passes and 4-tube passes heat exchanger is used to heat glycerin from 20°C to 50°C by hot water, which enters the thin-walled 2-cm-diameter tubes at 80°C and leaves at 40°C. The total length of the tubes in the heat exchanger is 60 m. The convection heat transfer coefficient is 25 W/m² · °C on the glycerin (shell) side and 160 W/m² · °C on the water (tube) side. Draw the heat exchanger and determine the

rate of heat transfer in the heat exchanger (a) before any fouling occurs and (b) after fouling with a fouling factor of $0.0006 \text{ m}^2 \cdot ^\circ\text{C}/\text{W}$ occurs on the outer surfaces of the tubes. Note take Correction factor $F=0.9$.

Solution

$$A_s = \pi DL = \pi(0.02 \text{ m})(60 \text{ m}) = 3.77 \text{ m}^2$$

$$\dot{Q} = UA_s F \Delta T_{\text{lm}, CF}$$

where F is the correction factor and $\Delta T_{\text{lm}, CF}$ is the log mean temperature difference for the counter-flow arrangement. These two quantities are determined from

$$\begin{aligned}\Delta T_1 &= T_{h, \text{in}} - T_{c, \text{out}} = (80 - 50)^\circ\text{C} = 30^\circ\text{C} \\ \Delta T_2 &= T_{h, \text{out}} - T_{c, \text{in}} = (40 - 20)^\circ\text{C} = 20^\circ\text{C} \\ \Delta T_{\text{lm}, CF} &= \frac{\Delta T_1 - \Delta T_2}{\ln(\Delta T_1/\Delta T_2)} = \frac{30 - 20}{\ln(30/20)} = 24.7^\circ\text{C}\end{aligned}$$

(a) In the case of no fouling, the overall heat transfer coefficient U is determined from

$$U = \frac{1}{\frac{1}{h_i} + \frac{1}{h_o}} = \frac{1}{\frac{1}{160 \text{ W/m}^2 \cdot ^\circ\text{C}} + \frac{1}{25 \text{ W/m}^2 \cdot ^\circ\text{C}}} = 21.6 \text{ W/m}^2 \cdot ^\circ\text{C}$$

Then the rate of heat transfer becomes

$$\dot{Q} = UA_s F \Delta T_{\text{lm}, CF} = (21.6 \text{ W/m}^2 \cdot ^\circ\text{C})(3.77 \text{ m}^2)(0.91)(24.7^\circ\text{C}) = \mathbf{1830 \text{ W}}$$

(b) When there is fouling on one of the surfaces, the overall heat transfer coefficient U is

$$\begin{aligned}U &= \frac{1}{\frac{1}{h_i} + \frac{1}{h_o} + R_f} = \frac{1}{\frac{1}{160 \text{ W/m}^2 \cdot ^\circ\text{C}} + \frac{1}{25 \text{ W/m}^2 \cdot ^\circ\text{C}} + 0.0006 \text{ m}^2 \cdot ^\circ\text{C}/\text{W}} \\ &= 21.3 \text{ W/m}^2 \cdot ^\circ\text{C}\end{aligned}$$

The rate of heat transfer in this case becomes

$$\dot{Q} = UA_s F \Delta T_{\text{lm}, CF} = (21.3 \text{ W/m}^2 \cdot ^\circ\text{C})(3.77 \text{ m}^2)(0.91)(24.7^\circ\text{C}) = \mathbf{1805 \text{ W}}$$

*With best wishes
Dr. Mohamed Ramadan*