

1-a) For the block diagram shown in Figure 1, draw the equivalent signal flow graph using 5 nodes: input, output, and nodes a, b, and c.

Use masson rule to find the transfer function of the system.



- 1-b) Consider the system below in figure 2 and let p=0.
 - i) Determine conditions on K and z so that the system is stable.
 - ii) Determine all possible conditions on K and z so that the system will be marginally stable



Figure 2

- 2- a) Consider the block diagram in figure 3.
 - (a) With $G_c(s) = 1$, r(t)=0, and d(t)=unit step, find the range of gain K such that the steady state output due to the disturbance d(t) is 0.05d(t).
 - (b) Let d(t)=0. With $KG_c(s) = i g$, find the steady state step error. Also find the steady state ramp error.
 - (c) What effect would $G_c(s) = \frac{1}{s}$ have on the steady state errors? Note: check the root locus first.



Figure 3

For the system given, find the jw-axis crossing point and the corresponding value of K.

b) User the Routh-Hurwitz criteria to determine the number of roots in the left half complex plane, the right half plane, and on the jw-axis for each of the following polynomials .

1-
$$d(s) = s^3 + s^4 + 2s^3 + 2s^2 + s + 1$$

ii-
$$d(s) = s^4 + 9s^3 + 45s^2 + 87s + 50$$

iii- $d(s) = s^6 + 5s^5 + 14s^4 + 40s^3 + 64s^2 + 80s + 96$

3-a)

Hand sketch the root locus of 1 + KG(s) = 0 as K varies from 0 to $+\infty$, where

$$G(s) = \frac{s+2}{s(s+1)(s+3)^2}$$

Make sure you provide verbal description on the following: open-loop pole/zero map; real

axis decision; and asymptotes.

3-b) For the control system shown in Fig.4, find the following :

- i) The damping ratio, ζ .
- ii) The settling time in response to a step input.
- iii) c(t), t > 0 for r is unit step and c(0) = 0
- iv) The steady state output in response to $r(t) = \cos 2t$.

$$r(t) \xrightarrow{s+3} c(t)$$
Figure 4

4-a) Given the straight line Bode diagram of magnitude in figure5, find the corresponding transfer function.





4-b) For the system given below in figure 6, estimate the values of K and K_t so that a maximum percentage overshoot of 9.6% and a settling time of 0.05 sec for a tolerance band of 1% are achieved.



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c) Consider the standard feedback system shown below in figure 7.



Figure 7

Let the transfer function of the plant is $G_p(s) = \frac{1}{s(s+5)}$,

Design a PI controller whose T.F of the form $Gc(s) = k_p + \frac{k_i}{s}$ such that

such that the closed loop system is stable with one pole at $r_1 = -4$ and the other two poles are at $r_{2,3} = -\zeta \omega_o \pm j \omega_o \sqrt{1-\zeta^2}$ with $\omega_o \ge 2$, $\zeta > 0$, and ζ is as large as possible. Draw the Bode plots of the system with and without controller.

Good Luck

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Model Answer of The Final Corrective Exam

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1-a)





FOR P=0, the characteristic equation is given by: $S^{2}(S^{2}+2S+8) + K(S+Z) = 0$ $S^{4}+2S^{3}+8S^{2}+KS+KZ=0$ Construct the Huwarth array

L

For stable systen 16 > K > 0, Z > 0 $(16k-k^2 - 2kz)(2)$ 16-k > 0 16-K-2z > 0 16 > k + 2zii For marginally stable system Put S = jo $officulton^4 - 2jo^3 - 8o^2 + jko + kz = 0$ $-2 officulton^3 + ko = 0$ $officulton^4 + (2z-8)o^2 + z = 0$ $officulton^4 + (2z-8)$

2-a)

Consider the block diagram below.

(a) With $G_c(s) = 1$, r(t)=0, and d(t)=unit step, find the range of gain K such that the steady state output due to the disturbance d(t) is 0.05d(t).

(b) Let d(t)=0. With $KG_c(s) = fg$, find the steady state step error. Also find the steady state ramp error.

(c) What effect would
$$G_{c}(s) = \frac{1}{s}$$
 are on the stady state error? Note: there the root local far.

$$i^{+}(t) + \frac{k}{(s+t)} = \frac{1}{(s-t)(s-2)} = \frac{1}{(s-t)(s-2)} = \frac{1}{(s-t)(s-2)}$$

$$i^{+}(t) = \frac{1}{(s-t)(s-2)} = \frac{1}{(s-t)(s-2)} = \frac{1}{(s-t)(s-2)} = \frac{1}{(s-t)(s-2)}$$

$$i^{+}(t) = \frac{1}{(s-t)(s-2)} = \frac{1}{(s-t)(s-2)} = \frac{1}{(s-t)(s-2)} = \frac{1}{(s-t)(s-2)}$$

$$i^{+}(t) = \frac{1}{(s-t)(s-2)} =$$

Stable, Number of poles on the Imaginary line = 4

ii)			
S ⁴	1	45	50
S ³	9	87	0
S ²	35.33	50	
S	74.26	0	
S ⁰	50		

The system is stable with all four poles on the left half plane

iii)				
S	1	14	64	96
S	5	40	80	0
S⁴	6	48	96	
S ³	0	0		
	2 4	96		
S ²	4	16		
S	0	0		
	8	0		
S ⁰	16			
5	TO			

The system is stable with 2 pole in the LHP and 4 on the imaginary ax

3)

a) Hand sketch the root locus of 1 + KG(s) = 0 as K varies from 0 to $+\infty$, where

$$G(s) = \frac{s+2}{s(s+1)(s+3)^2}$$

$$\implies open loop poled are o, -1, -3, -3$$

$$\implies 7272 - are -2 =$$
Number of asymptoted are are $-2 =$

$$Number of asymptoted arg le = \frac{(2k+1)\pi}{3} = 60^{\circ}, 180^{\circ}, 300^{\circ}$$
Intersection of asymptoted and real axis

$$\begin{aligned} x &= \frac{\sum p \cdot k_3 - \sum \omega_{k,3}}{n-m} = \frac{-i_1 - 3 - 3 + 2}{3} = -\frac{5}{3} \\ The charackeristic eqn. is \\ 1 + KGim = c \implies 1 + \frac{K(s+2)}{(s^{r_2} + s)(s^{r_2} + 6S + 9)} = c \\ s'^4 + 7s^3 + 15s^{r_2} + 9s^r + ks + 2k = c \\ Construct The array. \\ s'^4 + 1 = 15 = 2K \\ s'^2 + \frac{7}{4} - (9+k) = c \\ s'^2 + \frac{15 - 9k - 9}{76} - 2^{i_1}K \\ s' + \frac{(9-9k)(9+k) - 98k}{96 - 9k} = c \\ 1 + \frac{2K}{76} - \frac{96}{7} \\ (96 - 9k)(9+k) - 98k > c = s \\ E64 - 81k - 98k - 9k^2 > c \\ E64 - 81k - 98k - 9k^2 > c \\ E64 - 179k - 9k^2 > c \\ K \leq 4, \\ Frie K = 4 \\ The Auxilierry Equinis \frac{60}{7} K^2 + 8 = c \\ s'' = \pm c_1 \frac{16}{15} \int_{-15}^{15} \frac{p_{cint}s}{p_{cint}s} \\ intersect \\ The Integring \\ = \pm c_1 9(6) \end{bmatrix}$$



3-b)

$$r(t) = \frac{s+3}{s^2+7s+10} - c(t)$$

$$2 \int W_n = 7 \quad w_n^2 = 10 \implies W_n = \sqrt{10} = 3.16$$

$$S = \frac{7}{2.W_n} = \frac{7}{2(3.16)} = \frac{1.107}{1.107} \implies OVERDOMPED$$

$$System \implies NegArrive, Road, Distrivet Roots, Distrivet Roots, Sort, Road, Distrivet Roots, Sort, So$$

4-a)



4 - b)

For the system given below in figure 5, estimate the values of K and K_t so that a maximum percentage overshoot of 9.6% and a settling time of 0.05 sec for a tolerance band of 1% are achieved.



The system is reduced to



c) Consider the standard feedback system shown below in figure 6.





The characteristic Eq. is given right

$$1 + G_{c}(s) G_{p}(s) = 0$$

 $1 + \frac{k_{p}s' + kc}{s'} \frac{1}{(s'^{2} + 5s)} = 0$
 $s'^{3} + 5s^{2} + kps' + kc = 0$
 $s' = -4$ satisfies The eq. 1.
 $-64 + 80 - 4kp + kc = 0$
 $16' - 4kp + kc = 0$
 $16' - 4kp + kc = 0$
 $kc = 4kp - 16$
 $kp > 4$
 $(s'^{3} + 4s^{2}) + (s'^{-16}) + kp(s+4) = 0$
 $s'^{2} (s'+4) + (s'+4)(s-4) + kp(s+4) = 0$
 $s'^{2} (s'+4) + (s'+4)(s-4) + kp(s+4) = 0$
 $s'' + 4s - \frac{1}{2} + \frac{1}{3} [kp^{-\frac{17}{4}} = -\frac{1}{5} w_{n} + \frac{1}{3} w_{n}] - \frac{1}{5}^{2}$
 $\frac{1}{4} (1 - \frac{2}{5}^{2}) = kp - \frac{17}{4} = \frac{15}{4} + \frac{17}{4} = kp = 3$

istic Ean. is given by:





The required B0de diagram